



6. (10p) If $L = \lim_{n \rightarrow +\infty} \frac{3+6+9+\dots+3(n-1)}{n^2+5}$, then L is:

- a. $\frac{5}{2}$
- b. 1
- c. 2
- d. 3
- e. $\frac{3}{2}$

7. (10p) Let $f: \mathbb{R} \rightarrow \mathbb{R}$, $f(x) = \begin{cases} a \ln(3-x), & x \leq 1 \\ \frac{2^x-2}{x-1}, & x > 1 \end{cases}$, with $a \in \mathbb{R}^*$. The value of the parameter a such that f is continuous at $x = 1$ is:

- a. 1
- b. 0.5
- c. $\ln 2$
- d. $\ln 3$
- e. 2

8. (10p) Let $f: [0, +\infty) \rightarrow (0, +\infty)$ such that $f(x) + f(1-x) = 1$ for all $x \in [0, +\infty)$ and the sequences of real numbers $a_n = \sum_{k=1}^{n-1} f\left(\frac{n-k}{n}\right)$, $b_n = \ln \frac{a_n}{n}$, $n \geq 3$. If $L = \lim_{n \rightarrow +\infty} b_n$, then L is:

- a. 0
- b. $\ln \frac{1}{2}$
- c. ∞
- d. 1
- e. $\ln 2$

9. (5p) Let $f: \mathbb{R} \rightarrow \mathbb{R}$, $f(x) = x^2 + mx + n$, such that the image of f verifies $\text{Im } f = \left[-\frac{9}{4}, +\infty\right)$ and f has the global extreme point at $x = 2.5$. If $S = m + n$, then S is:

- a. 1
- b. 0
- c. -1
- d. 2
- e. -2

10. (5p) Consider the system of equations

$$\begin{cases} mx + m^2y - z = m^2 \\ x - my + z = 2 \\ x - y + z = -1 \end{cases}, \quad \text{where } m \in \mathbb{R}.$$

The system is incompatible for:

- a. $m = -1$
- b. $m = 0$
- c. $m \neq -1$
- d. $m \neq 1$
- e. $m = 1$



MULTIPLE-CHOICE TEST
in MATHEMATICS

1. (10p) Let $f: [0, 3] \rightarrow \mathbb{R}$, $f(x) = \begin{cases} 2x, & x \in [0, 1] \\ x^2 + 2x, & x \in (1, 3] \end{cases}$. Then $\int_0^2 f(x) dx$ is equal to:

- a. $\frac{17}{3}$
- b. $\frac{20}{3}$
- c. $\frac{19}{3}$
- d. $\frac{19}{2}$
- e. $\frac{53}{3}$

2. (10p) The definite integral $\int_0^2 \left(\frac{3x-1}{x^2-2x-3} \right) dx$ is equal to:

- a. $-\ln 3$
- b. $5\ln 5$
- c. $3\ln 5$
- d. $-5 + \ln 5$
- e. $5\ln 3$

3. (10p) Let $f: \mathbb{R} \rightarrow \mathbb{R}$, $f(x) = e^{-mx}$, $m \in \mathbb{R}^*$. Then $f''(x) + 4f'(x) + 3f(x) < 0$ if and only if:

- a. $m \in (2, 3)$
- b. $m \in (1, 2)$
- c. $m \in (0, 3)$
- d. $m \in (1, 3)$
- e. $m \in (1, 4)$

4. (10p) Let $f: \mathbb{R} \rightarrow \mathbb{R}$, $f(x) = \begin{cases} e^{ax} + 1, & x < 0 \\ \ln(x+1) + b, & x \geq 0 \end{cases}$, with $a, b \in \mathbb{R}$.

If $A = \{(a, b) \in \mathbb{R}^2 \mid f \text{ admits a derivative on } \mathbb{R}\}$ and $S = \sum_{(a,b) \in A} (a^2 + b^2)$, then:

- a. $S = 15$
- b. $S = 10$
- c. $S = 13$
- d. $S = 17$
- e. $S = 5$

5. (10p) The abscisse of the minimum point of the function

$$f: \mathbb{R} \rightarrow \mathbb{R}, f(x) = \max\{x + 2, -2x + 2\}$$

is equal to:

- a. $x = 0$
- b. $x = -1$
- c. $x = \frac{3}{2}$
- d. $x = 1$
- e. $x = 4$



MULTIPLE-CHOICE TEST
in MATHEMATICS

1. (10p) Let $f: \mathbb{R} \rightarrow \mathbb{R}$, $f(x) = \begin{cases} a \ln(3-x), & x \leq 1 \\ \frac{2^x-2}{x-1}, & x > 1 \end{cases}$, with $a \in \mathbb{R}^*$. The value of the parameter a such that f is continuous at $x = 1$ is:
- 0.5
 - 1
 - 2
 - $\ln 2$
 - $\ln 3$
2. (10p) Let $f: [0, 3] \rightarrow \mathbb{R}$, $f(x) = \begin{cases} 2x, & x \in [0, 1] \\ x^2 + 2x, & x \in (1, 3] \end{cases}$. Then $\int_0^2 f(x) dx$ is equal to:
- $\frac{20}{3}$
 - $\frac{17}{3}$
 - $\frac{19}{3}$
 - $\frac{2}{19}$
 - $\frac{53}{3}$
3. (10p) Let $f: \mathbb{R} \rightarrow \mathbb{R}$, $f(x) = e^{-mx}$, $m \in \mathbb{R}^*$. Then $f''(x) + 4f'(x) + 3f(x) < 0$ if and only if:
- $m \in (1, 3)$
 - $m \in (1, 2)$
 - $m \in (0, 3)$
 - $m \in (2, 3)$
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- 0
 - $\ln 2$
 - ∞
 - $\ln \frac{1}{2}$
 - 1
5. (10p) The abscisse of the minimum point of the function
 $f: \mathbb{R} \rightarrow \mathbb{R}$, $f(x) = \max\{x+2, -2x+2\}$
is equal to:
- $x = 4$
 - $x = -1$
 - $x = 0$
 - $x = \frac{3}{2}$
 - $x = 1$
6. (10p) The definite integral $\int_0^2 \left(\frac{3x-1}{x^2-2x-3} \right) dx$ is equal to:



- a. $5\ln 3$
- b. $3\ln 5$
- c. $-\ln 3$
- d. $-5 + \ln 5$
- e. $5\ln 5$

7. (10p) If $L = \lim_{n \rightarrow +\infty} \frac{3+6+9+\dots+3(n-1)}{n^2+5}$, then L is:

- a. $\frac{5}{2}$
- b. $\frac{3}{2}$
- c. 1
- d. 3
- e. 2

8. (5p) Consider the system of equations

$$\begin{cases} mx + m^2y - z = m^2 \\ x - my + z = 2 \\ x - y + z = -1 \end{cases}, \quad \text{where } m \in \mathbb{R}.$$

The system is incompatible for:

- a. $m \neq 1$
- b. $m = 1$
- c. $m \neq -1$
- d. $m = -1$
- e. $m = 0$

9. (5p) Let $f: \mathbb{R} \rightarrow \mathbb{R}$, $f(x) = x^2 + mx + n$, such that the image of f verifies $\text{Im } f = [-\frac{9}{4}, +\infty)$ and f has the global extreme point at $x = 2.5$. If $S = m + n$, then S is:

- a. 1
- b. 2
- c. 0
- d. -2
- e. -1

10. (10p) Let $f: \mathbb{R} \rightarrow \mathbb{R}$, $f(x) = \begin{cases} e^{ax} + 1, & x < 0 \\ \ln(x+1) + b, & x \geq 0 \end{cases}$, with $a, b \in \mathbb{R}$.

If $A = \{(a, b) \in \mathbb{R}^2 \mid f \text{ admits a derivative on } \mathbb{R}\}$ and $S = \sum_{(a,b) \in A} (a^2 + b^2)$, then:

- a. $S = 5$
- b. $S = 10$
- c. $S = 15$
- d. $S = 13$
- e. $S = 17$



MULTIPLE-CHOICE TEST
in MATHEMATICS

1. (10p) Let $f: [0, +\infty) \rightarrow (0, +\infty)$ such that $f(x) + f(1-x) = 1$ for all $x \in [0, +\infty)$ and the sequences of real numbers $a_n = \sum_{k=1}^{n-1} f\left(\frac{n-k}{n}\right)$, $b_n = \ln \frac{a_n}{n}$, $n \geq 3$. If $L = \lim_{n \rightarrow +\infty} b_n$, then L is:

- a. $\ln \frac{1}{2}$
- b. ∞
- c. 0
- d. 1
- e. $\ln 2$

2. (10p) The definite integral $\int_0^2 \left(\frac{3x-1}{x^2-2x-3} \right) dx$ is equal to:

- a. $3\ln 5$
- b. $5\ln 5$
- c. $-\ln 3$
- d. $-5 + \ln 5$
- e. $5\ln 3$

3. (5p) Consider the system of equations

$$\begin{cases} mx + m^2y - z = m^2 \\ x - my + z = 2 \\ x - y + z = -1 \end{cases}, \quad \text{where } m \in \mathbb{R}.$$

The system is incompatible for:

- a. $m = 0$
- b. $m = -1$
- c. $m \neq -1$
- d. $m = 1$
- e. $m \neq 1$

4. (10p) Let $f: \mathbb{R} \rightarrow \mathbb{R}$, $f(x) = \begin{cases} e^{ax} + 1, & x < 0 \\ \ln(x+1) + b, & x \geq 0 \end{cases}$, with $a, b \in \mathbb{R}$.

If $A = \{(a, b) \in \mathbb{R}^2 \mid f \text{ admits a derivative on } \mathbb{R}\}$ and $S = \sum_{(a,b) \in A} (a^2 + b^2)$, then:

- a. $S = 15$
- b. $S = 5$
- c. $S = 10$
- d. $S = 17$
- e. $S = 13$

5. (10p) Let $f: \mathbb{R} \rightarrow \mathbb{R}$, $f(x) = e^{-mx}$, $m \in \mathbb{R}^*$. Then $f''(x) + 4f'(x) + 3f(x) < 0$ if and only if:

- a. $m \in (2, 3)$
- b. $m \in (1, 3)$
- c. $m \in (0, 3)$
- d. $m \in (1, 2)$
- e. $m \in (1, 4)$

6. (10p) If $L = \lim_{n \rightarrow +\infty} \frac{3+6+9+\dots+3(n-1)}{n^2+5}$, then L is:



- a. 1
- b. $\frac{5}{2}$
- c. $\frac{3}{2}$
- d. 2
- e. 3

7. (10p) The abscisse of the minimum point of the function

$$f: \mathbf{R} \rightarrow \mathbf{R}, f(x) = \max\{x + 2, -2x + 2\}$$

is equal to:

- a. $x = \frac{3}{2}$
- b. $x = -1$
- c. $x = 1$
- d. $x = 0$
- e. $x = 4$

8. (10p) Let $f: \mathbf{R} \rightarrow \mathbf{R}, f(x) = \begin{cases} a \ln(3 - x), & x \leq 1 \\ \frac{2^x - 2}{x - 1}, & x > 1 \end{cases}$, with $a \in \mathbf{R}^*$. The value of the parameter a such that f is continuous at $x = 1$ is:

- a. 2
- b. 0.5
- c. 1
- d. $\ln 2$
- e. $\ln 3$

9. (5p) Let $f: \mathbf{R} \rightarrow \mathbf{R}, f(x) = x^2 + mx + n$, such that the image of f verifies $\text{Im } f = [-\frac{9}{4}, +\infty)$ and f has the global extreme point at $x = 2.5$. If $S = m + n$, then S is:

- a. 0
- b. 1
- c. 2
- d. -1
- e. -2

10. (10p) Let $f: [0, 3] \rightarrow \mathbf{R}, f(x) = \begin{cases} 2x, & x \in [0, 1] \\ x^2 + 2x, & x \in (1, 3] \end{cases}$. Then $\int_0^2 f(x) dx$ is equal to:

- a. $\frac{19}{2}$
- b. $\frac{17}{3}$
- c. $\frac{20}{3}$
- d. $\frac{53}{3}$
- e. $\frac{19}{3}$



MULTIPLE-CHOICE TEST
in MATHEMATICS

1. (5p) Consider the system of equations

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The system is incompatible for:

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- c. $m = 1$
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2. (10p) Let $f: [0, 3] \rightarrow \mathbf{R}$, $f(x) = \begin{cases} 2x, & x \in [0, 1] \\ x^2 + 2x, & x \in (1, 3] \end{cases}$. Then $\int_0^2 f(x) dx$ is equal to:

- a. $\frac{19}{2}$
- b. $\frac{20}{3}$
- c. $\frac{19}{3}$
- d. $\frac{17}{3}$
- e. $\frac{53}{3}$

3. (10p) The abscisse of the minimum point of the function

$$f: \mathbf{R} \rightarrow \mathbf{R}, f(x) = \max\{x + 2, -2x + 2\}$$

is equal to:

- a. $x = 1$
- b. $x = -1$
- c. $x = \frac{3}{2}$
- d. $x = 4$
- e. $x = 0$

4. (10p) The definite integral $\int_0^2 \left(\frac{3x-1}{x^2-2x-3} \right) dx$ is equal to:

- a. $3\ln 5$
- b. $-\ln 3$
- c. $-5 + \ln 5$
- d. $5\ln 3$
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5. (10p) If $L = \lim_{n \rightarrow +\infty} \frac{3+6+9+\dots+3(n-1)}{n^2+5}$, then L is:

- a. 2
- b. $\frac{5}{2}$
- c. 1



- d. $\frac{3}{2}$
e. 3

6. (10p) Let $f: \mathbb{R} \rightarrow \mathbb{R}$, $f(x) = \begin{cases} a \ln(3-x), & x \leq 1 \\ \frac{2^x-2}{x-1}, & x > 1 \end{cases}$, with $a \in \mathbb{R}^*$. The value of the parameter a such that f is continuous at $x = 1$ is:

- a. 0.5
b. 1
c. $\ln 3$
d. 2
e. $\ln 2$

7. (10p) Let $f: \mathbb{R} \rightarrow \mathbb{R}$, $f(x) = e^{-mx}$, $m \in \mathbb{R}^*$. Then $f''(x) + 4f'(x) + 3f(x) < 0$ if and only if:

- a. $m \in (1, 3)$
b. $m \in (1, 2)$
c. $m \in (0, 3)$
d. $m \in (1, 4)$
e. $m \in (2, 3)$

8. (5p) Let $f: \mathbb{R} \rightarrow \mathbb{R}$, $f(x) = x^2 + mx + n$, such that the image of f verifies $\text{Im } f = [-\frac{9}{4}, +\infty)$ and f has the global extreme point at $x = 2.5$. If $S = m + n$, then S is:

- a. 1
b. -1
c. 2
d. -2
e. 0

9. (10p) Let $f: [0, +\infty) \rightarrow (0, +\infty)$ such that $f(x) + f(1-x) = 1$ for all $x \in [0, +\infty)$ and the sequences of real numbers $a_n = \sum_{k=1}^{n-1} f\left(\frac{n-k}{n}\right)$, $b_n = \ln \frac{a_n}{n}$, $n \geq 3$. If $L = \lim_{n \rightarrow +\infty} b_n$, then L is:

- a. 0
b. 1
c. ∞
d. $\ln 2$
e. $\ln \frac{1}{2}$

10. (10p) Let $f: \mathbb{R} \rightarrow \mathbb{R}$, $f(x) = \begin{cases} e^{ax} + 1, & x < 0 \\ \ln(x+1) + b, & x \geq 0 \end{cases}$, with $a, b \in \mathbb{R}$.

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- a. $S = 15$
b. $S = 5$
c. $S = 13$
d. $S = 17$
e. $S = 10$



MULTIPLE-CHOICE TEST
in MATHEMATICS

1. (10p) The definite integral $\int_0^2 \left(\frac{3x-1}{x^2-2x-3} \right) dx$ is equal to:
- a. $5\ln 5$
 - b. $-5 + \ln 5$
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2. (10p) The abscisse of the minimum point of the function
 $f: \mathbb{R} \rightarrow \mathbb{R}, f(x) = \max\{x + 2, -2x + 2\}$
is equal to:
- a. $x = -1$
 - b. $x = 4$
 - c. $x = \frac{3}{2}$
 - d. $x = 1$
 - e. $x = 0$
3. (10p) Let $f: [0, 3] \rightarrow \mathbb{R}, f(x) = \begin{cases} 2x, & x \in [0, 1] \\ x^2 + 2x, & x \in (1, 3] \end{cases}$. Then $\int_0^2 f(x) dx$ is equal to:
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 - d. $\frac{53}{3}$
 - e. $\frac{20}{3}$
4. (10p) If $L = \lim_{n \rightarrow +\infty} \frac{3+6+9+\dots+3(n-1)}{n^2+5}$, then L is:
- a. 1
 - b. $\frac{5}{2}$
 - c. 2
 - d. $\frac{3}{2}$
 - e. 3
5. (10p) Let $f: \mathbb{R} \rightarrow \mathbb{R}, f(x) = \begin{cases} a \ln(3-x), & x \leq 1 \\ \frac{2^x-2}{x-1}, & x > 1 \end{cases}$, with $a \in \mathbb{R}^*$. The value of the parameter a such that f is continuous at $x = 1$ is:
- a. $\ln 3$
 - b. 1
 - c. 0.5
 - d. 2
 - e. $\ln 2$



6. (5p) Consider the system of equations

$$\begin{cases} mx + m^2y - z = m^2 \\ x - my + z = 2 \\ x - y + z = -1 \end{cases}, \quad \text{where } m \in \mathbb{R}.$$

The system is incompatible for:

- a. $m = 0$
- b. $m = -1$
- c. $m = 1$
- d. $m \neq -1$
- e. $m \neq 1$

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- a. $\ln \frac{1}{2}$
- b. 0
- c. $\ln 2$
- d. ∞
- e. 1

9. (10p) Let $f: \mathbb{R} \rightarrow \mathbb{R}$, $f(x) = \begin{cases} e^{ax} + 1, & x < 0 \\ \ln(x+1) + b, & x \geq 0 \end{cases}$, with $a, b \in \mathbb{R}$.

If $A = \{(a, b) \in \mathbb{R}^2 \mid f \text{ admits a derivative on } \mathbb{R}\}$ and $S = \sum_{(a,b) \in A} (a^2 + b^2)$, then:

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- a. 0
- b. 1
- c. 2
- d. -1
- e. -2



MULTIPLE-CHOICE TEST
in MATHEMATICS

1. (5p) Let $f: \mathbb{R} \rightarrow \mathbb{R}$, $f(x) = x^2 + mx + n$, such that the image of f verifies $\text{Im } f = [-\frac{9}{4}, +\infty)$ and f has the global extreme point at $x = 2.5$. If $S = m + n$, then S is:

- a. -1
- b. 0
- c. 2
- d. -2
- e. 1

2. (10p) Let $f: \mathbb{R} \rightarrow \mathbb{R}$, $f(x) = \begin{cases} a \ln(3-x), & x \leq 1 \\ \frac{2^x-2}{x-1}, & x > 1 \end{cases}$, with $a \in \mathbb{R}^*$. The value of the parameter a such that f is continuous at $x = 1$ is:

- a. $\ln 2$
- b. 1
- c. 0.5
- d. 2
- e. $\ln 3$

3. (10p) Let $f: \mathbb{R} \rightarrow \mathbb{R}$, $f(x) = \begin{cases} e^{ax} + 1, & x < 0 \\ \ln(x+1) + b, & x \geq 0 \end{cases}$, with $a, b \in \mathbb{R}$.

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- c. $m \in (1, 2)$
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- a. $\frac{20}{3}$
- b. $\frac{17}{3}$
- c. $\frac{19}{2}$
- d. $\frac{19}{3}$
- e. $\frac{53}{3}$



6. (10p) If $L = \lim_{n \rightarrow +\infty} \frac{3+6+9+\dots+3(n-1)}{n^2+5}$, then L is:

- a. 1
- b. $\frac{5}{2}$
- c. 3
- d. $\frac{3}{2}$
- e. 2

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is equal to:

- a. $x = 1$
- b. $x = \frac{3}{2}$
- c. $x = -1$
- d. $x = 4$
- e. $x = 0$

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- a. 0
- b. ∞
- c. $\ln \frac{1}{2}$
- d. $\ln 2$
- e. 1

9. (5p) Consider the system of equations

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- a. $m = -1$
- b. $m = 1$
- c. $m = 0$
- d. $m \neq -1$
- e. $m \neq 1$

10. (10p) The definite integral $\int_0^2 \left(\frac{3x-1}{x^2-2x-3} \right) dx$ is equal to:

- a. $5\ln 3$
- b. $3\ln 5$
- c. $5\ln 5$
- d. $-\ln 3$
- e. $-5 + \ln 5$